

Supplementary Material for “Extending Classification Algorithms to Case-Control Studies”

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Within Pair Symmetry of the Conditional Classifiers

As stated in the manuscript, for the 1:1 case-control setting, the conditional-Gaussian naive Bayes classifier and linear discriminant analysis are guaranteed to classify one case and one control per strata.

Gaussian Naive Bayes

If individual 1 in strata i is classified as a case according to the conditional naive Bayes classifier, then individual 2 in strata i will be classified as a control.

Proof. Let x_{ijk} denote feature $k = 1, \dots, K$ for individual $j = 1, \dots, g$ in case-control strata $i = 1, \dots, n$ where g is the group size and n is the number of strata. The response to be modeled is denote y_{ij} where $y_{ij} = 1$ if individual j in strata i is a case and 0 otherwise. For the 1:1 case-control grouping, $g = 2$ and $j \in \{1, 2\}$ and the total number of individuals in the sample is $N = 2n$.

After adjusting for the case control pairing, $x_{i1k} = -x_{i2k}$ and $y_{i1} = 1 - y_{i2}$ for all i and k . It follows that $\hat{\mu}_{1k} = -\hat{\mu}_{2k}$ (see below) and $\sigma_{1k}^2 = \sigma_{2k}^2$ for all k (see below). Therefore, $p(x_{i1k}|C_1) = \phi(x_{i1k}; \hat{\mu}_{1k}, \sigma_{1k}^2) = \phi(-x_{i1k}; -\hat{\mu}_{1k}, \sigma_{1k}^2) = \phi(x_{i2k}; \hat{\mu}_{2k}, \sigma_{2k}^2) = p(x_{i2k}|C_2)$. Suppose that individual y_{i1} is predicted to be a case, i.e., $p(\text{Case}) \prod_{k=1}^K p(x_{i1k}|\text{Case}) > p(\text{Control}) \prod_{k=1}^K p(x_{i1k}|\text{Control})$. Because $p(\text{Case}) = p(\text{Control})$ then

$$\begin{aligned} & \prod_{k=1}^K p(x_{i1k}|\text{Case}) > \prod_{k=1}^K p(x_{i1k}|\text{Control}) \\ \implies & \prod_{k=1}^K p(x_{i2k}|\text{Control}) > \prod_{k=1}^K p(x_{i2k}|\text{Case}) \\ \implies & \hat{y}_{i2} = \text{Control} \end{aligned}$$

thus the predictions for group i contain one case and one control. This occurs with probability 1 because the “equality” condition has probability 0.

Here we justify the claim that $\hat{\mu}_{1k} = -\hat{\mu}_{2k}$:

$$\begin{aligned}
\hat{\mu}_{1k} &= \frac{1}{n} \sum_{i=1}^n \sum_{j=1}^2 \mathbf{1}(y_{ij} = 1) x_{ijk} = \frac{1}{n} \sum_{i=1}^n [\mathbf{1}(y_{i1} = 1) x_{i1k} + \mathbf{1}(y_{i2} = 1) x_{i2k}] \\
&= \frac{1}{n} \sum_{i=1}^n [\mathbf{1}(1 - y_{i2} = 1)(-x_{i2k}) + \mathbf{1}(1 - y_{i1} = 1)(-x_{i1k})] \\
&= \frac{1}{n} \sum_{i=1}^n [\mathbf{1}(y_{i2} = 0)(-x_{i2k}) + \mathbf{1}(y_{i1} = 0)(-x_{i1k})] = \frac{-1}{n} \sum_{i=1}^n \sum_{j=1}^2 \mathbf{1}(y_{ij} = 0) x_{ijk} \\
&= -\hat{\mu}_{2k}.
\end{aligned}$$

Similar techniques can be used to show $\sigma_{1k}^2 = \sigma_{2k}^2$. □

Linear Discriminant Analysis

If individual 1 in strata i is classified as a case according to conditional linear discriminant analysis, then individual 2 in strata i will be classified as a control.

Proof. Using the same notation from the proof for the Gaussian naive Bayes classifier, individual 1 in strata i is classified as a case, i.e., $\hat{y}_{i1} = 1$, if

$$\log \left(\frac{Pr(y_{i1} = 1 | \mathbf{x}_{i1})}{Pr(y_{i1} = 0 | \mathbf{x}_{i1})} \right) = \log \left(\frac{\pi_1 \phi(\mathbf{x}_{i1}; \boldsymbol{\mu}_1, \boldsymbol{\Sigma})}{\pi_0 \phi(\mathbf{x}_{i1}; \boldsymbol{\mu}_0, \boldsymbol{\Sigma})} \right) > 0 \quad (1)$$

where π_1 and π_0 are the proportion of individuals in the case and control groups, respectively, $\boldsymbol{\mu}_1$ and $\boldsymbol{\mu}_0$ are the mean vector for the case and control groups, respectively, and $\boldsymbol{\Sigma}$ is the variance covariance matrix that is assumed to be the same in both groups. As before $\boldsymbol{\mu}_0 = -\boldsymbol{\mu}_1$ and the assumption that a single variance covariance matrix $\boldsymbol{\Sigma}$ can be used is guaranteed to be satisfied. Further, due to the balance in cases and controls, $\pi_1 = \pi_0 = 0.5$. Therefore, (1) can be rewritten

$$\begin{aligned}
\log \left(\frac{\pi_1 \phi(\mathbf{x}_{i1}; \boldsymbol{\mu}_1, \boldsymbol{\Sigma})}{\pi_0 \phi(\mathbf{x}_{i1}; \boldsymbol{\mu}_0, \boldsymbol{\Sigma})} \right) &= \log [\phi(\mathbf{x}_{i1}; \boldsymbol{\mu}_1, \boldsymbol{\Sigma}) - \log (\phi(\mathbf{x}_{i1}; \boldsymbol{\mu}_0, \boldsymbol{\Sigma})] + \log \left(\frac{\pi_1}{\pi_0} \right) \\
&= \mathbf{x}_{i1}^\top \boldsymbol{\Sigma}^{-1} (\boldsymbol{\mu}_1 - \boldsymbol{\mu}_0) - \frac{1}{2} (\boldsymbol{\mu}_1 + \boldsymbol{\mu}_0)^\top \boldsymbol{\Sigma}^{-1} (\boldsymbol{\mu}_1 - \boldsymbol{\mu}_0) + \log(1) \\
&= \mathbf{x}_{i1}^\top \boldsymbol{\Sigma}^{-1} (\boldsymbol{\mu}_1 - \boldsymbol{\mu}_0)
\end{aligned}$$

because $\boldsymbol{\mu}_1 + \boldsymbol{\mu}_0 = \mathbf{0}$ and $\log(1) = 0$.

Again from (1), individual 1 in strata i is classified as a case if $\mathbf{x}_{i1}^\top \boldsymbol{\Sigma}^{-1} (\boldsymbol{\mu}_1 - \boldsymbol{\mu}_0) > 0$, which implies $-\mathbf{x}_{i1}^\top \boldsymbol{\Sigma}^{-1} (\boldsymbol{\mu}_1 - \boldsymbol{\mu}_0) = \mathbf{x}_{i2}^\top \boldsymbol{\Sigma}^{-1} (\boldsymbol{\mu}_1 - \boldsymbol{\mu}_0) < 0$ and therefore individual 2 in strata i is classified as a control. □

CLR is Special Case of Proposed Methods

We also claimed that the pair corrected and standard CLR methods are mathematically equivalent, which we prove here in two steps. First we show that the conditional likelihood is unaffected by this pair correction.

Proof. Let $\mathbf{x}_{ij}$ represent the k -dimensional feature vector for individual $j \in \{1, 2\}$ in stratum $i = 1, \dots, n$. CLR maximizes the conditional likelihood given by

$$L_{CLR}(\beta|\mathbf{X}, \mathbf{y}) = \prod_{i=1}^n P(y_{i1} = 1, y_{i2} = 0 | \mathbf{x}_{i1}, \mathbf{x}_{i2}, y_{i1} + y_{i2} = 1) = \prod_{i=1}^n \frac{\exp(\beta^\top \mathbf{x}_{i1})}{\sum_{j=1}^2 \exp(\beta^\top \mathbf{x}_{ij})}. \quad (2)$$

For each stratum i , replace the raw feature vectors $\mathbf{x}_{ij}$ in (??) with the pair corrected feature vectors $\mathbf{x}_{ij}^* = \mathbf{x}_{ij} - \bar{\mathbf{x}}_i$. for $j = 1, 2$ gives the exact same likelihood for any pair i :

$$\begin{aligned} \frac{\exp(\beta^\top \mathbf{x}_{i1}^*)}{\exp(\beta^\top \mathbf{x}_{i2}^*) + \exp(\beta^\top \mathbf{x}_{i1}^*)} &= \frac{\exp[\beta^\top (\mathbf{x}_{i1} - \bar{\mathbf{x}}_i)]}{\exp[\beta^\top (\mathbf{x}_{i1} - \bar{\mathbf{x}}_i)] + \exp[\beta^\top (\mathbf{x}_{i1} - \bar{\mathbf{x}}_i)]} \\ &= \frac{\exp(\beta^\top \mathbf{x}_{i1} - \beta^\top \bar{\mathbf{x}}_i)}{\exp(\beta^\top \mathbf{x}_{i1} - \beta^\top \bar{\mathbf{x}}_i) + \exp(\beta^\top \mathbf{x}_{i1} - \beta^\top \bar{\mathbf{x}}_i)} \\ &= \frac{\exp(\beta^\top \mathbf{x}_{i1}) / \exp(\beta^\top \bar{\mathbf{x}}_i)}{\exp(\beta^\top \mathbf{x}_{i1}) / \exp(\beta^\top \bar{\mathbf{x}}_i) + \exp(\beta^\top \mathbf{x}_{i1}) / \exp(\beta^\top \bar{\mathbf{x}}_i)} \\ &= \frac{\exp(\beta^\top \mathbf{x}_{i1})}{\exp(\beta^\top \mathbf{x}_{i2}) + \exp(\beta^\top \mathbf{x}_{i2})}. \end{aligned}$$

Therefore, CLR is equivalent if the pair corrected or raw data are used to fit the model, i.e., $L_{CLR}(\beta|\mathbf{X}, \mathbf{y}) = L_{CLR}(\beta|\mathbf{X}^*, \mathbf{y})$. $\square$

We can now show that standard logistic regression applied to the pair corrected data is equivalent to the standard conditional logistic regression.

Proof. Let $\mathbf{x}_{ij}$ represent the k -dimensional feature vector for individual $j \in \{1, 2\}$ in stratum $i = 1, \dots, n$ and let $\mathbf{x}_{ij}^* = \mathbf{x}_{ij} - \bar{\mathbf{x}}_i$ represent the pair corrected version of $\mathbf{x}_{ij}$ for all i and j . It follows that $\mathbf{x}_{i1}^* = -\mathbf{x}_{i2}^*$. From above, the contribution of pair i to the likelihood maximized by conditional logistic regression is given by

$$\begin{aligned} \frac{\exp(\beta^\top \mathbf{x}_{i1})}{\exp(\beta^\top \mathbf{x}_{i1}) + \exp(\beta^\top \mathbf{x}_{i2})} &= \frac{\exp(\beta^\top \mathbf{x}_{i1}^*)}{\exp(\beta^\top \mathbf{x}_{i1}^*) + \exp(\beta^\top \mathbf{x}_{i2}^*)} \\ &= \frac{1}{1 + \exp(\beta^\top \mathbf{x}_{i2}^*) / \exp(\beta^\top \mathbf{x}_{i1}^*)} \\ &= \frac{1}{1 + \exp[\beta^\top (\mathbf{x}_{i2}^* - \mathbf{x}_{i1}^*)]} \\ &= \frac{1}{1 + \exp(2\beta^\top \mathbf{x}_{i2}^*)} \end{aligned}$$

The likelihood of standard logistic regression (without an intercept) for the pair corrected data is given by

$$L_{LR}(\boldsymbol{\beta}|\mathbf{X}^*, \mathbf{y}) = \prod_{i=1}^n \prod_{j=1}^2 \left(\frac{1}{1 + \exp(-\boldsymbol{\beta}^\top \mathbf{x}_{ij}^*)} \right)^{y_{ij}} \left(\frac{1}{1 + \exp(\boldsymbol{\beta}^\top \mathbf{x}_{ij}^*)} \right)^{1-y_{ij}}.$$

As defined, $y_{i1} = 1$ and $y_{i2} = 0$ for all i . Therefore, the intercept free logistic regression likelihood can be written

$$\begin{aligned} L_{LR}(\boldsymbol{\beta}|\mathbf{X}^*, \mathbf{y}) &= \prod_{i=1}^n \left(\frac{1}{1 + \exp(-\boldsymbol{\beta}^\top \mathbf{x}_{i1}^*)} \right) \left(\frac{1}{1 + \exp(\boldsymbol{\beta}^\top \mathbf{x}_{i2}^*)} \right) \\ &= \prod_{i=1}^n \left(\frac{1}{1 + \exp(\boldsymbol{\beta}^\top \mathbf{x}_{i2}^*)} \right) \left(\frac{1}{1 + \exp(\boldsymbol{\beta}^\top \mathbf{x}_{i2}^*)} \right) \\ &= \prod_{i=1}^n \left(\frac{1}{1 + \exp(\boldsymbol{\beta}^\top \mathbf{x}_{i2}^*)} \right)^2 \\ &= \left(\prod_{i=1}^n \frac{1}{1 + \exp(\boldsymbol{\beta}^\top \mathbf{x}_{i2}^*)} \right)^2 \\ &= [L_{CLR}(\boldsymbol{\beta}|\mathbf{X}^*/2, \mathbf{y})]^2 \end{aligned}$$

Suppose $\hat{\boldsymbol{\beta}}$ maximizes the conditional logistic likelihood, that is

$$\begin{aligned} \hat{\boldsymbol{\beta}} &= \operatorname{argmax}_{\boldsymbol{\beta} \in \mathbb{R}^k} L_{CLR}(\boldsymbol{\beta}|\mathbf{X}^*, \mathbf{y}) = \operatorname{argmax}_{\boldsymbol{\beta} \in \mathbb{R}^k} \prod_{i=1}^n \frac{1}{1 + \exp(2\boldsymbol{\beta}^\top \mathbf{x}_{i2}^*)} \text{ then} \\ 2\hat{\boldsymbol{\beta}} &= \operatorname{argmax}_{\boldsymbol{\beta} \in \mathbb{R}^k} \prod_{i=1}^n \frac{1}{1 + \exp(\boldsymbol{\beta}^\top \mathbf{x}_{i2}^*)} = \operatorname{argmax}_{\boldsymbol{\beta} \in \mathbb{R}^k} L_{CLR}(\boldsymbol{\beta}|\mathbf{X}^*/2, \mathbf{y}). \end{aligned}$$

Because $1/[1 + \exp(2\boldsymbol{\beta}^\top \mathbf{x}_{i2}^*)] \geq 0$ for all i , then the vector $\boldsymbol{\beta}$ that maximizes the likelihood function, also maximizes the square of the likelihood function, i.e.,

$$2\hat{\boldsymbol{\beta}} = \operatorname{argmax}_{\boldsymbol{\beta} \in \mathbb{R}^k} L_{CLR}(\boldsymbol{\beta}|\mathbf{X}^*/2, \mathbf{y}) = \operatorname{argmax}_{\boldsymbol{\beta} \in \mathbb{R}^k} L_{CLR}(\boldsymbol{\beta}|\mathbf{X}^*/2, \mathbf{y})^2 = \operatorname{argmax}_{\boldsymbol{\beta} \in \mathbb{R}^k} L_{LR}(\boldsymbol{\beta}|\mathbf{X}^*, \mathbf{y}).$$

Therefore, if $\boldsymbol{\beta}$ is the maximum likelihood estimator (MLE) for conditional logistic regression, then $2\boldsymbol{\beta}$ is the MLE for the logistic regression of the same data after centering each pair and setting the intercept to be 0. □

From these two proof we can conclude that the results obtained by fitting a standard conditional logistic regression to a dataset can be replicated exactly by fitting a standard logistic regression to the data corrected as we proposed in this manuscript (and scaling the regression coefficients appropriately). As such, we conclude that conditional logistic regression is a special case of the larger class of classification algorithms we proposed in this manuscript.

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